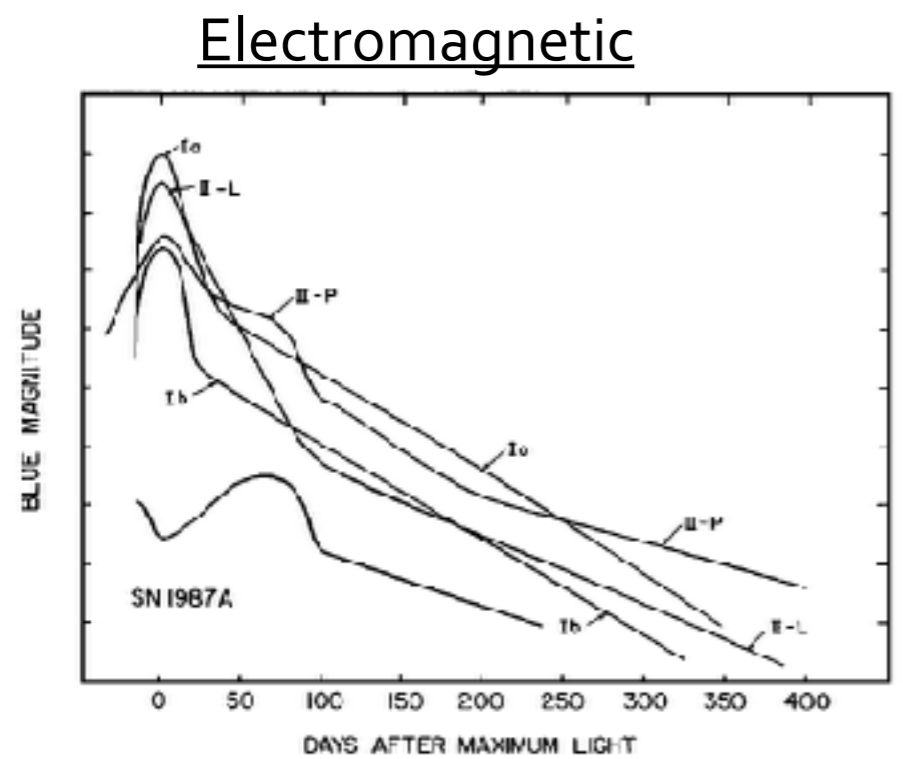
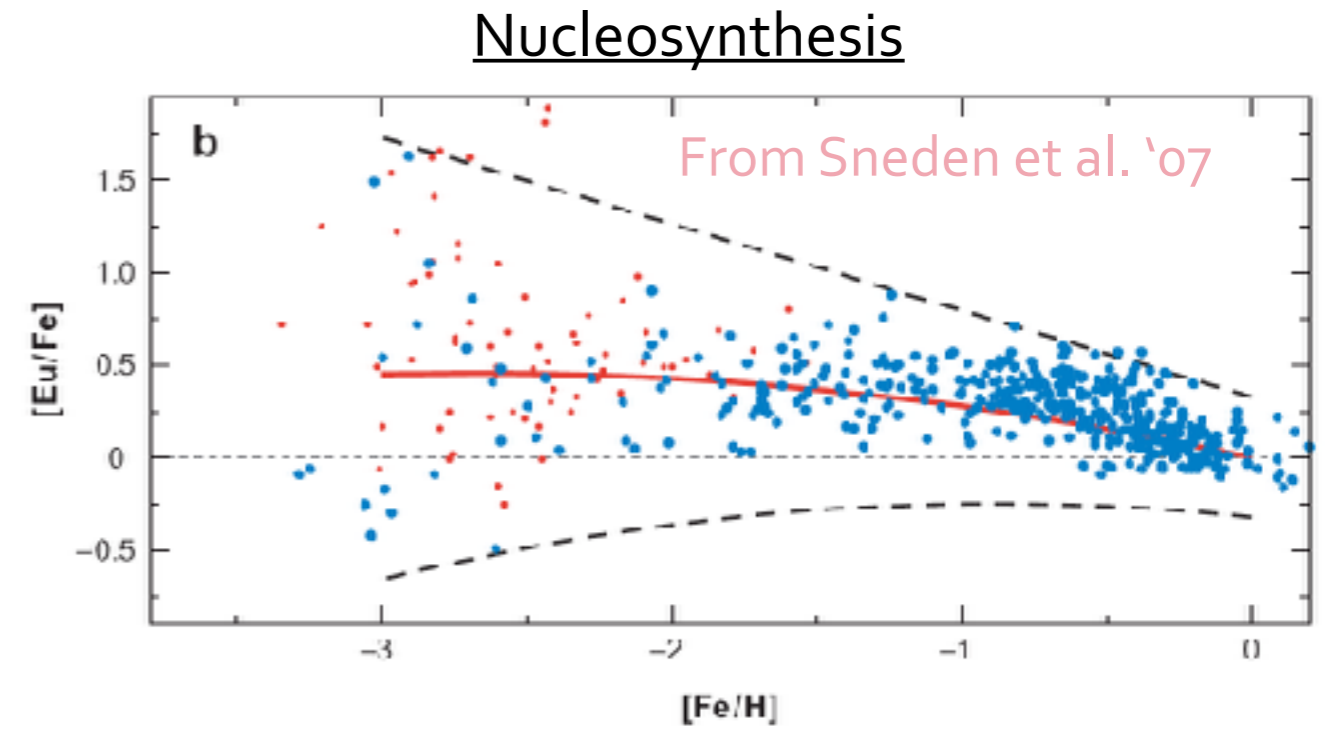
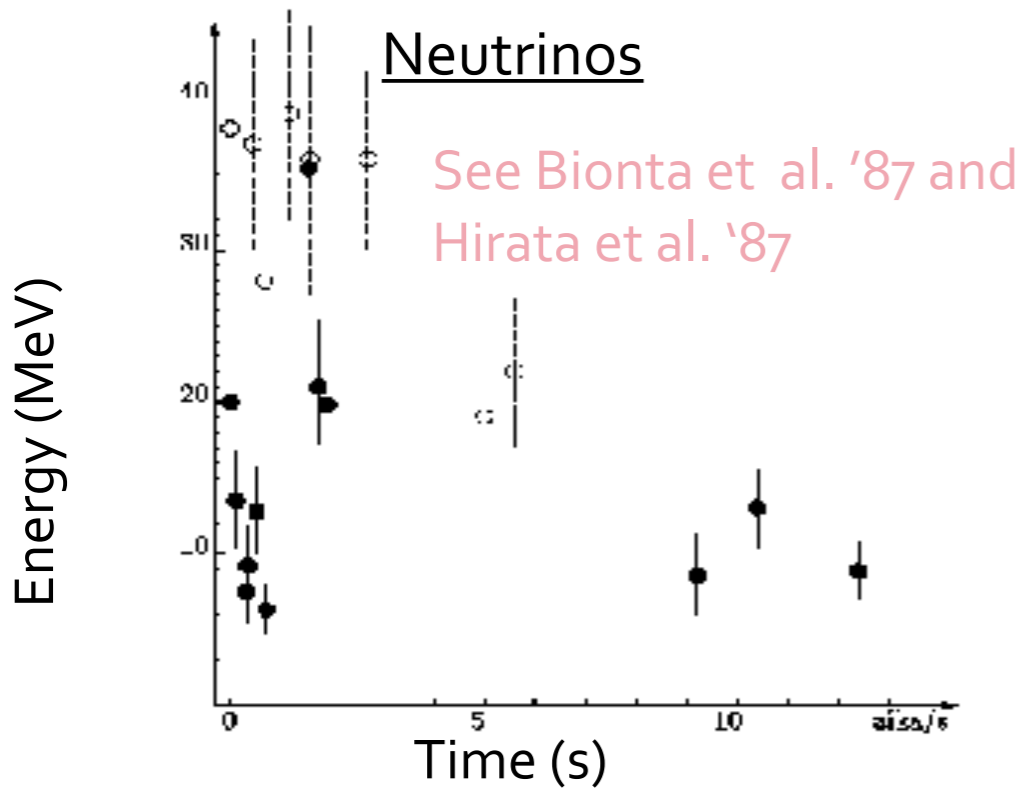


# The Impact of the Nuclear EoS on the Long Term Supernova Neutrino Signal

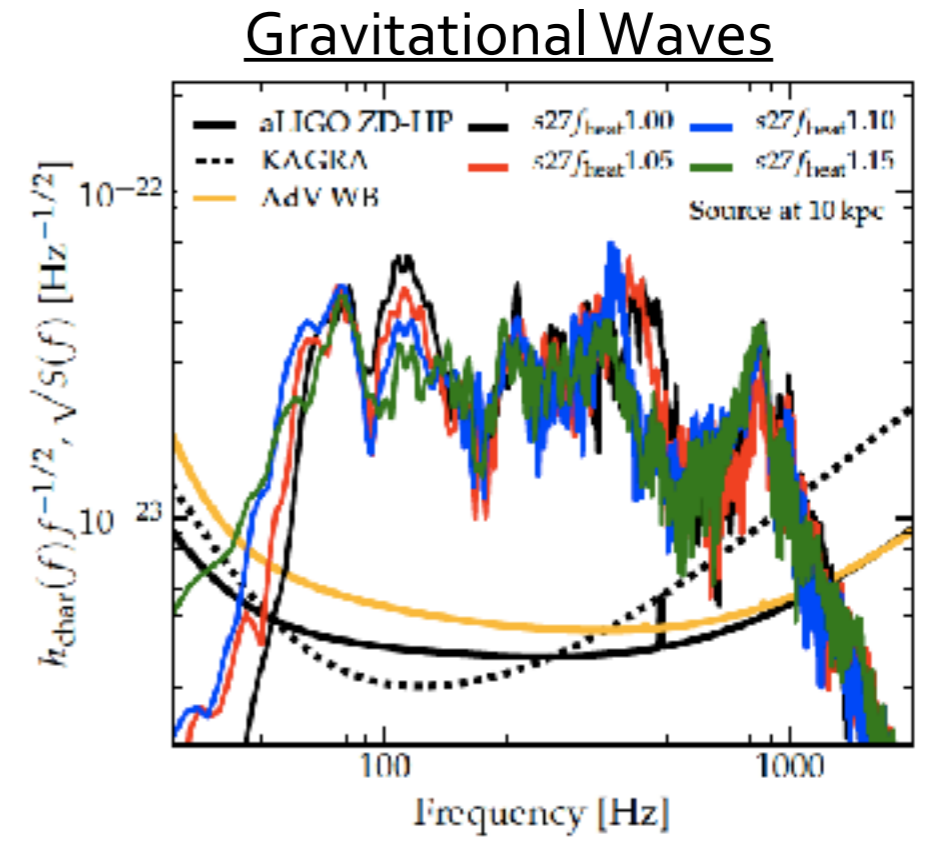
Luke Roberts  
NSCL, MSU

Collaborators: Sanjay Reddy, Andre  
Schneider, Gang Shen

# Core Collapse Supernovae: Multi-Messenger Events



From Filippenko '97



From Ott et al. '12

# Overview

- Background
- Impact of convection on neutrino emission
- Impact of opacities on neutrino emission and nucleosynthesis

# Milky Way Supernova Rate

- Most recent known MW CCSN  
Cas A (~300 yrs)
- Look for supernovae in  
galaxies analogous to MW  
(Cappellaro et al. 1999)
- Take census of historical  
galactic supernovae and  
correct for obscuration  
(Tammann et al. 1994)
- Reasonably consistent

multiply by  $\sim 2.4$  to get MW rate

galaxy type	Ia	rate [SNu] II+Ib/c	All
S0a-Sb	$0.27 \pm 0.08$	$0.63 \pm 0.24$	$0.91 \pm 0.26$
Sbc-Sd	$0.24 \pm 0.10$	$0.86 \pm 0.31$	$1.10 \pm 0.32$
Spirals*	$0.25 \pm 0.09$	$0.76 \pm 0.27$	$1.01 \pm 0.29$

Cappellaro et al. (1999)

# SN\* Neutrino Detectors

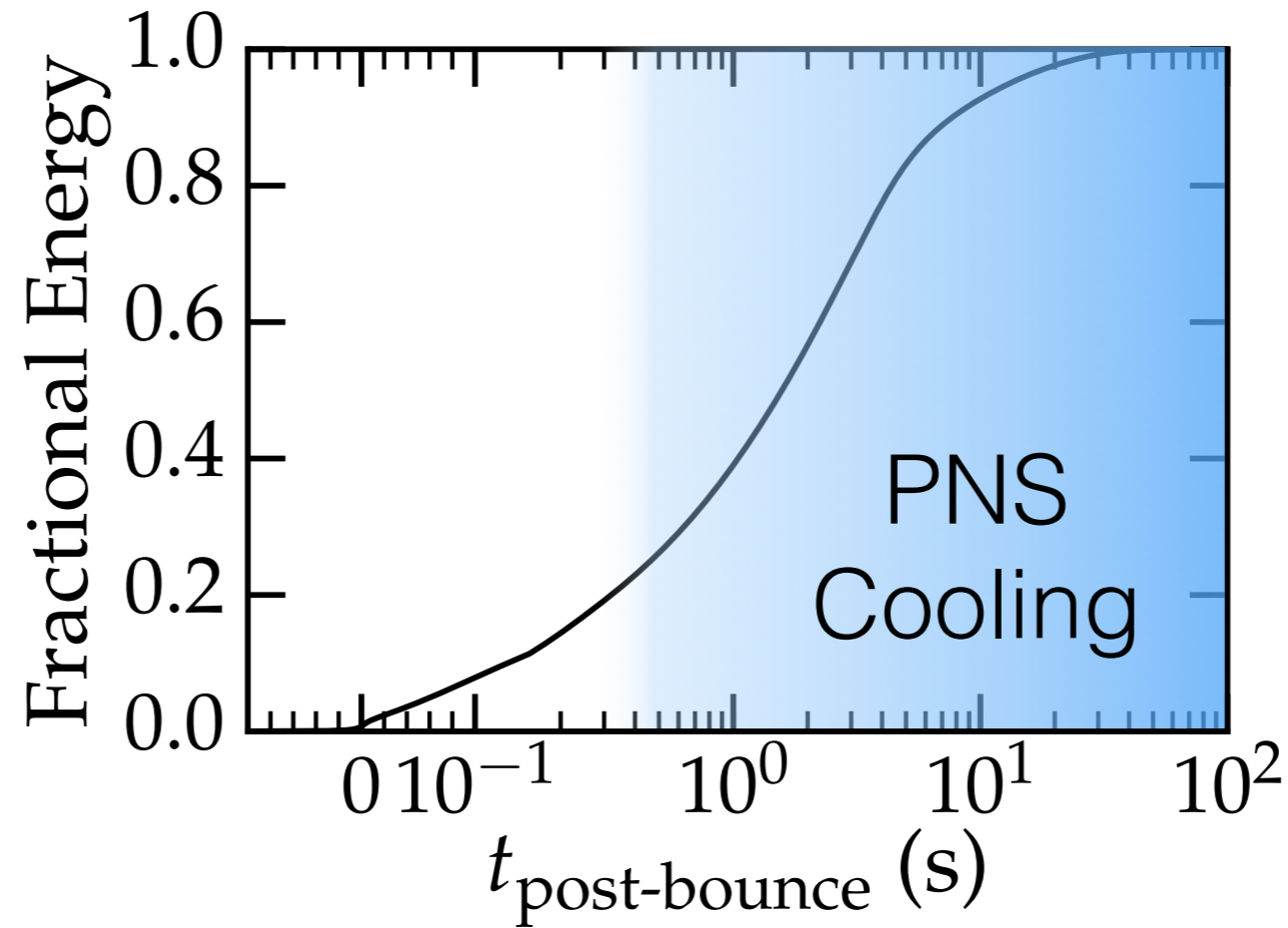
Detector	Type	Mass (kt)	Location	Events	Flavors	Status
Super-Kamiokande	H <sub>2</sub> O	32	Japan	7,000	$\bar{\nu}_e$	Running
LVD	C <sub>n</sub> H <sub>2n</sub>	1	Italy	300	$\bar{\nu}_e$	Running
KamLAND	C <sub>n</sub> H <sub>2n</sub>	1	Japan	300	$\bar{\nu}_e$	Running
Borexino	C <sub>n</sub> H <sub>2n</sub>	0.3	Italy	100	$\bar{\nu}_e$	Running
IceCube	Long string	(600)	South Pole	(10 <sup>6</sup> )	$\bar{\nu}_e$	Running
Baksan	C <sub>n</sub> H <sub>2n</sub>	0.33	Russia	50	$\bar{\nu}_e$	Running
MiniBooNE*	C <sub>n</sub> H <sub>2n</sub>	0.7	USA	200	$\bar{\nu}_e$	(Running)
HALO	Pb	0.08	Canada	30	$\nu_e, \nu_x$	Running
Daya Bay	C <sub>n</sub> H <sub>2n</sub>	0.33	China	100	$\bar{\nu}_e$	Running
NO $\nu$ A*	C <sub>n</sub> H <sub>2n</sub>	15	USA	4,000	$\bar{\nu}_e$	Turning on
SNO+	C <sub>n</sub> H <sub>2n</sub>	0.8	Canada	300	$\bar{\nu}_e$	Near future
MicroBooNE*	Ar	0.17	USA	17	$\nu_e$	Near future
DUNE	Ar	34	USA	3,000	$\nu_e$	Proposed
Hyper-Kamiokande	H <sub>2</sub> O	560	Japan	110,000	$\bar{\nu}_e$	Proposed
JUNO	C <sub>n</sub> H <sub>2n</sub>	20	China	6000	$\bar{\nu}_e$	Proposed
RENO-50	C <sub>n</sub> H <sub>2n</sub>	18	Korea	5400	$\bar{\nu}_e$	Proposed
LENA	C <sub>n</sub> H <sub>2n</sub>	50	Europe	15,000	$\bar{\nu}_e$	Proposed
PINGU	Long string	(600)	South Pole	(10 <sup>6</sup> )	$\bar{\nu}_e$	Proposed

Scholberg et al. (2015)

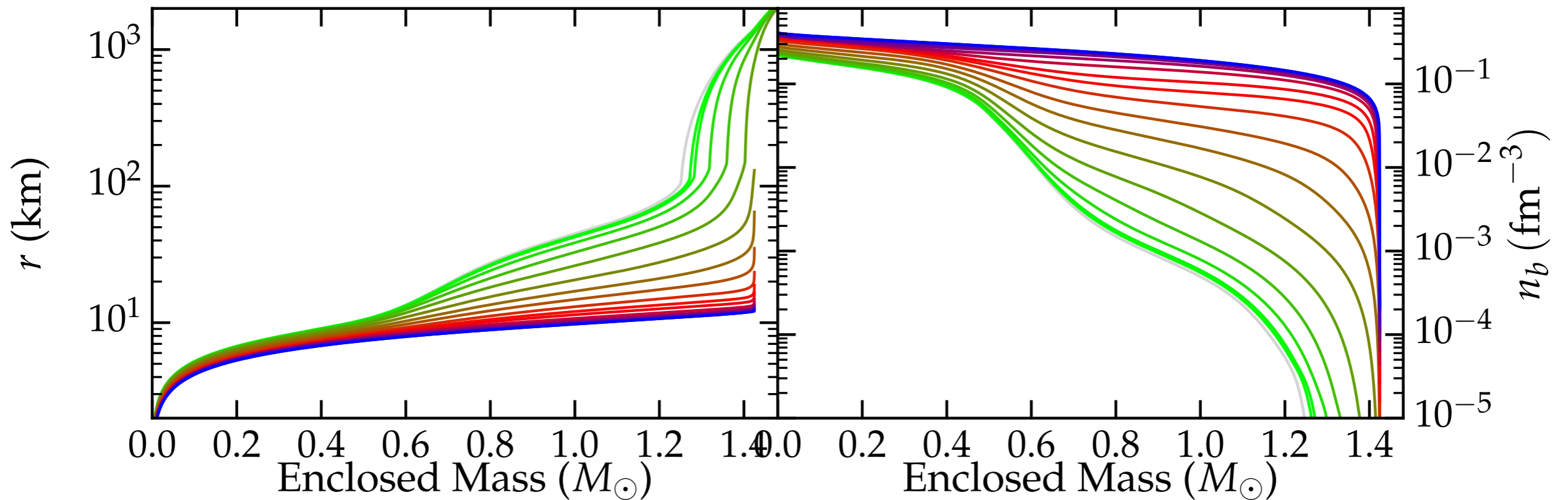
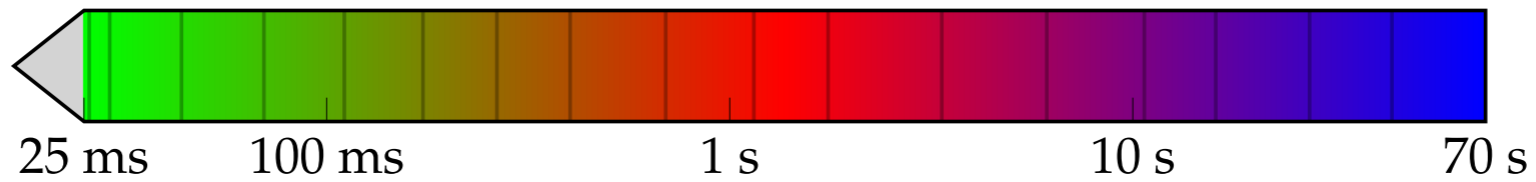
# Late Time SN Neutrino Emission

See e.g. Burrows & Lattimer '86, Pons et al. '99, Huedepohl et al. '10, Fischer et al. '10, LR '12

- Kelvin-Helmholtz evolution of the neutron star mediated by neutrinos
- Coupled neutron star structure and neutrino transport
- Sensitive to dense matter equation of state, neutrino oscillations
- Possibly cleaner problem than explosion mechanism

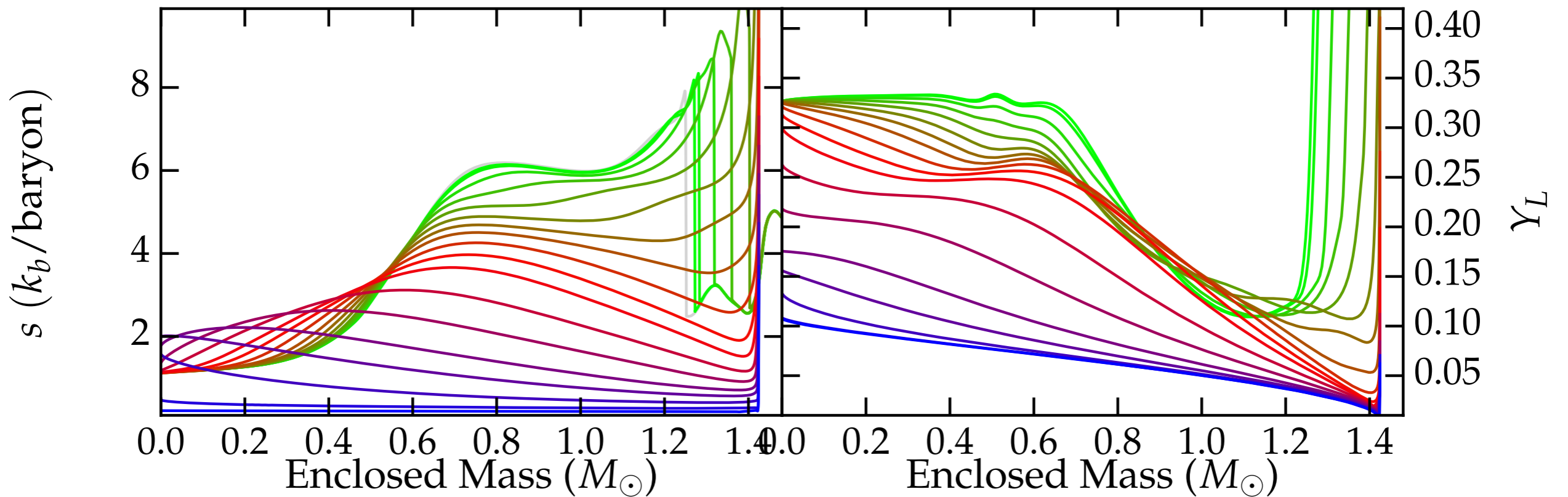
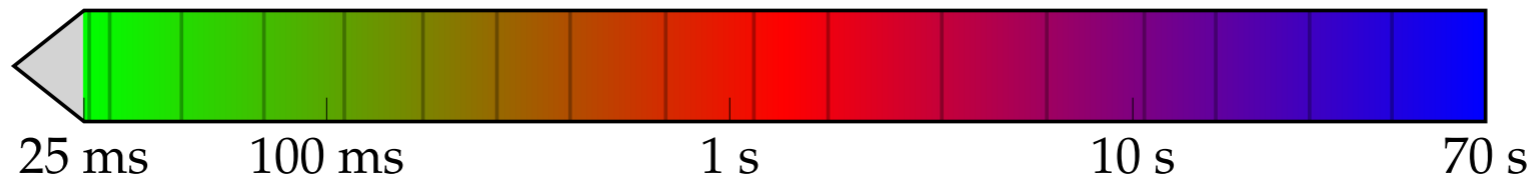


# Long Term PNS Evolution



$$E_{\text{SN}} \sim \frac{3GM_{\text{pns}}^2}{5r_{\text{NS}}} \approx 3 \times 10^{53} \text{ erg} \left( \frac{M_{\text{pns}}}{M_{\odot}} \right)^2 \left( \frac{r_{\text{NS}}}{12 \text{ km}} \right)^{-1}$$

# Long Term PNS Evolution

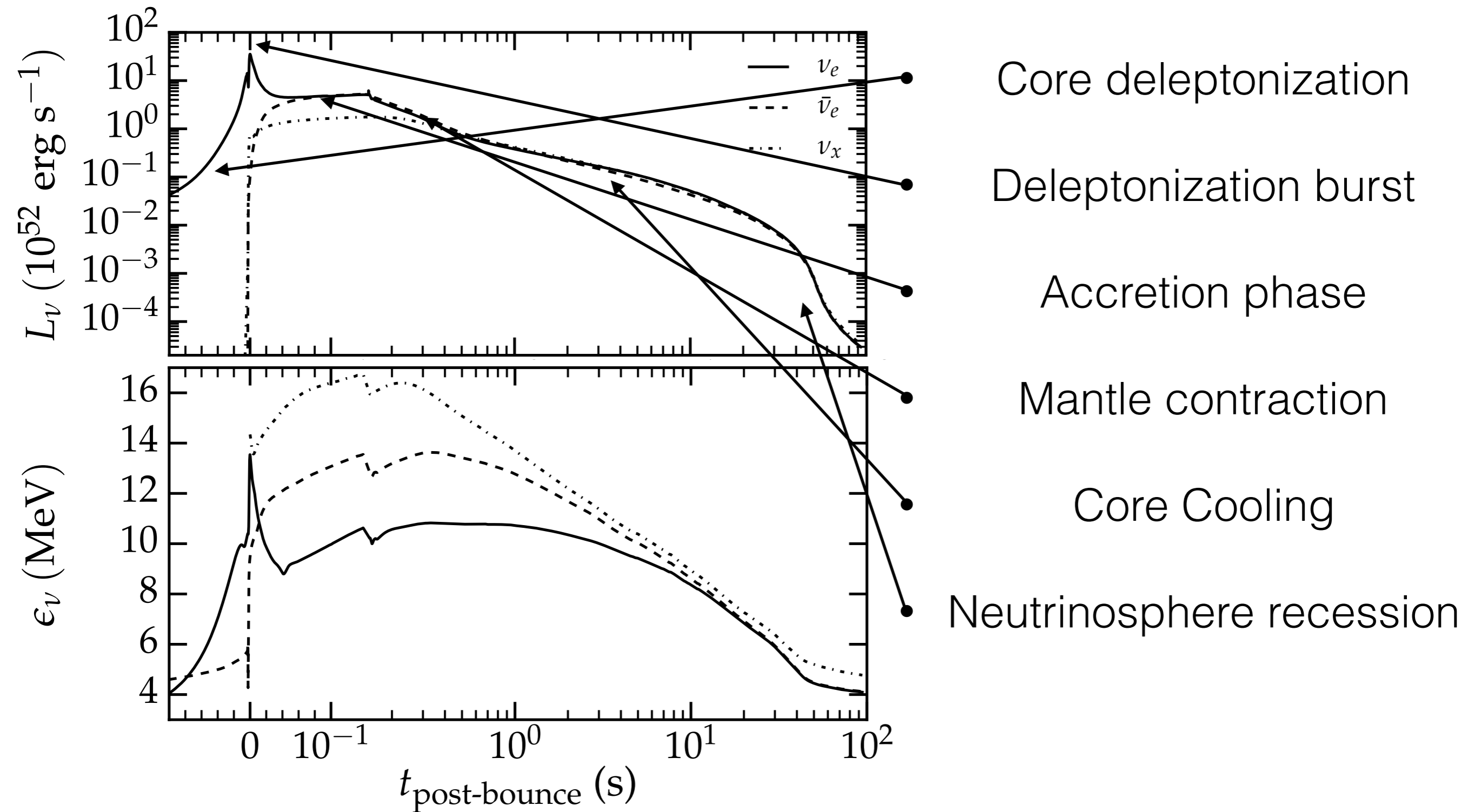


$$\tau_c \approx \frac{2\pi G_F^2 c_A^2}{\beta} \left\langle N_0 \frac{3n_b}{\pi^2} \frac{\partial s}{\partial T} \right\rangle k_B T_c R^2 \simeq 10 s \frac{k_B T_c}{30 \text{ MeV}} \frac{\langle n_b^{2/3} \rangle}{n_0^{2/3}} \left( \frac{R}{12 \text{ km}} \right)^2$$

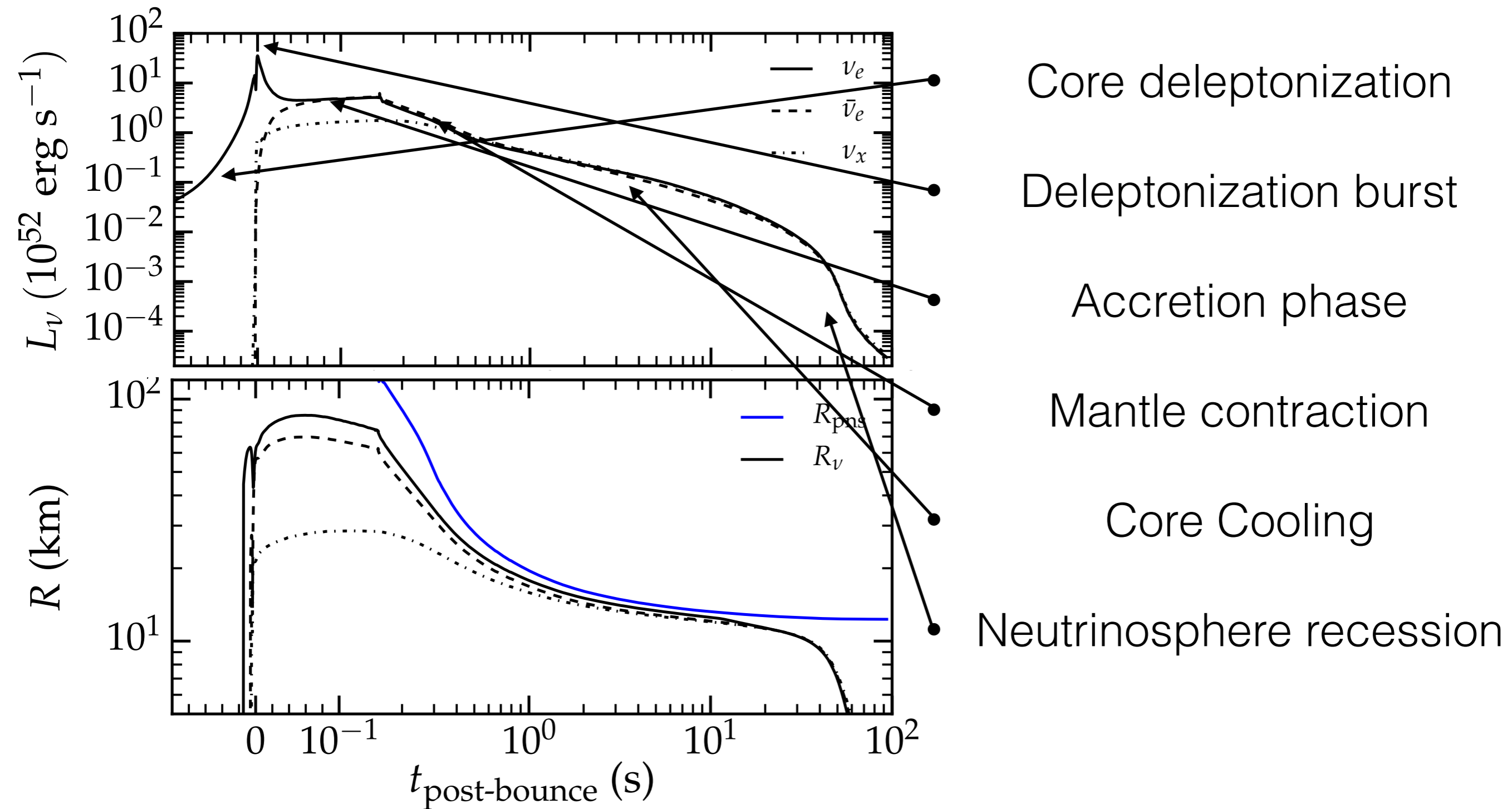
See Prakash et al. '97



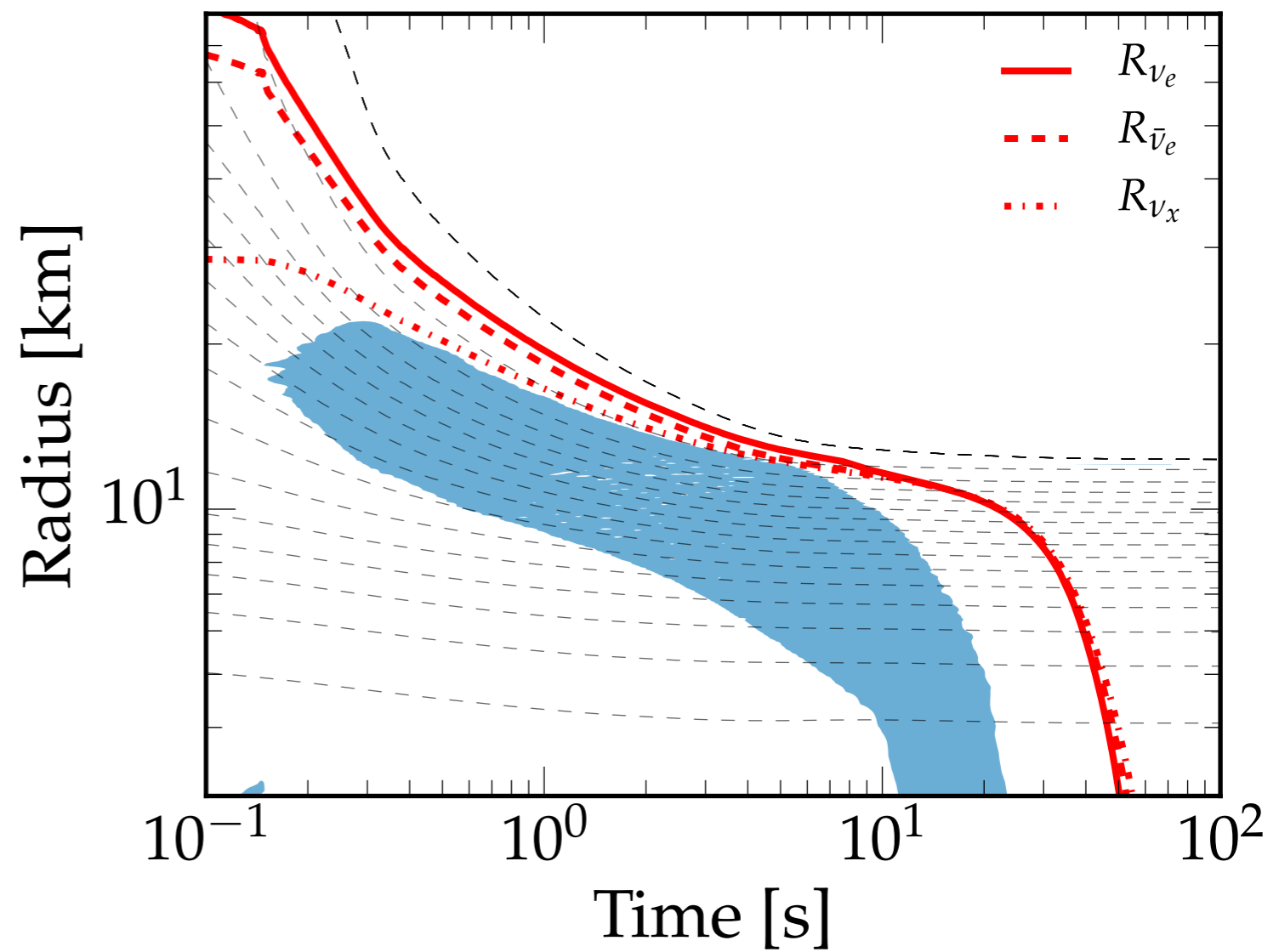
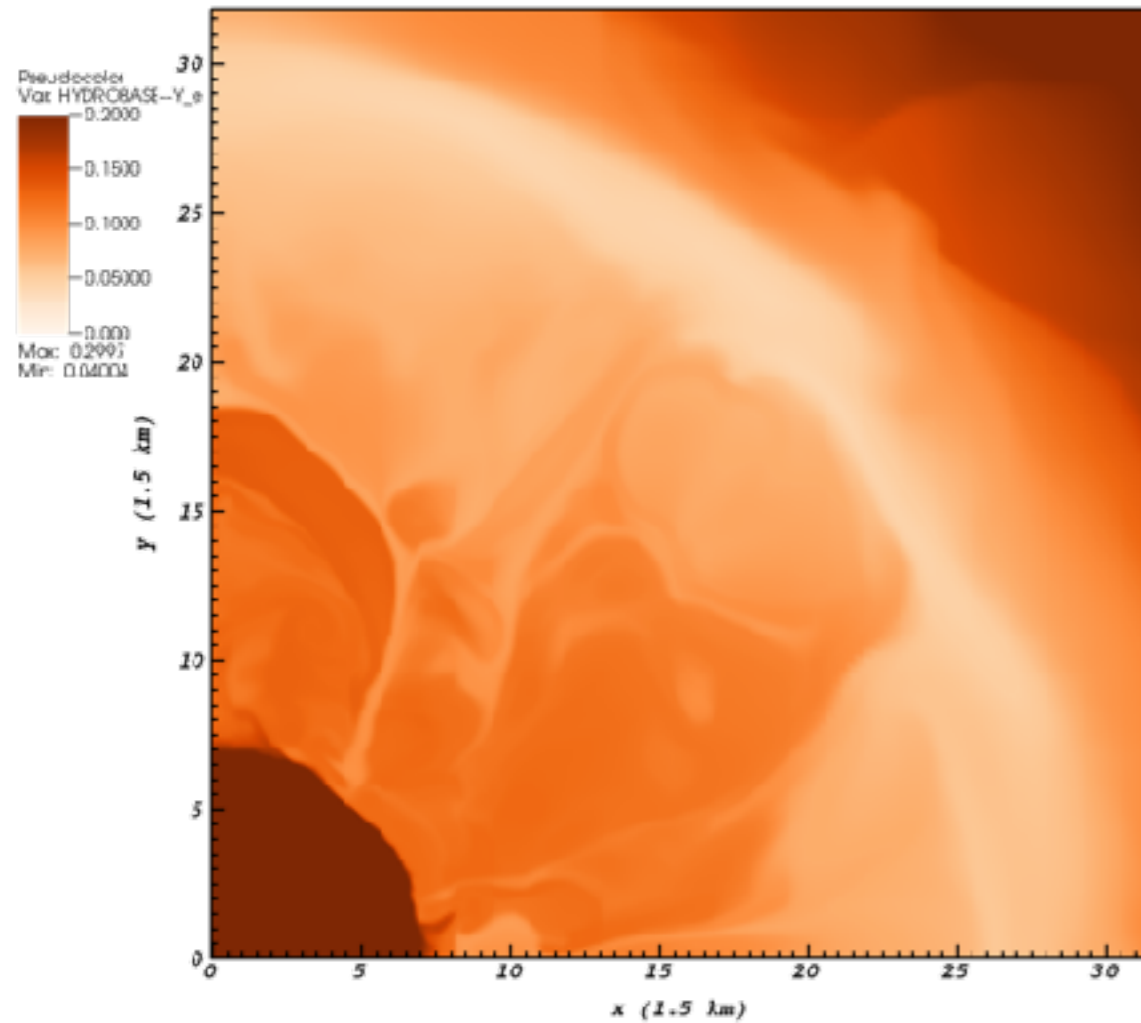
# Anatomy of the Neutrino Signal



# Anatomy of the Neutrino Signal



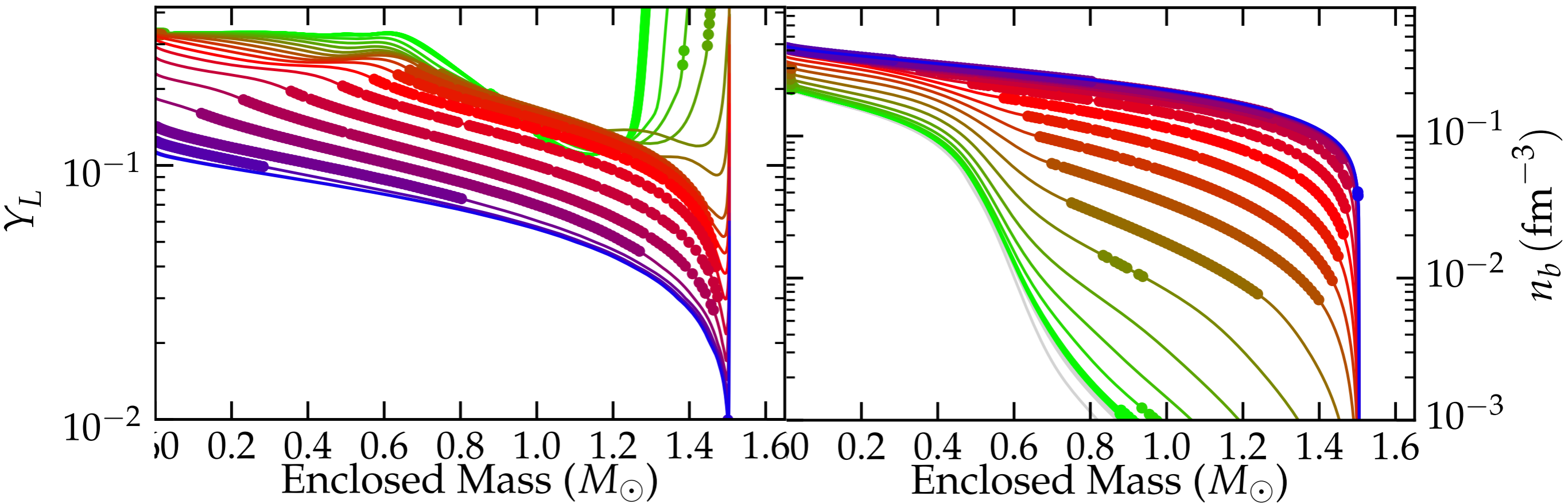
# Proto-Neutron Star Convection



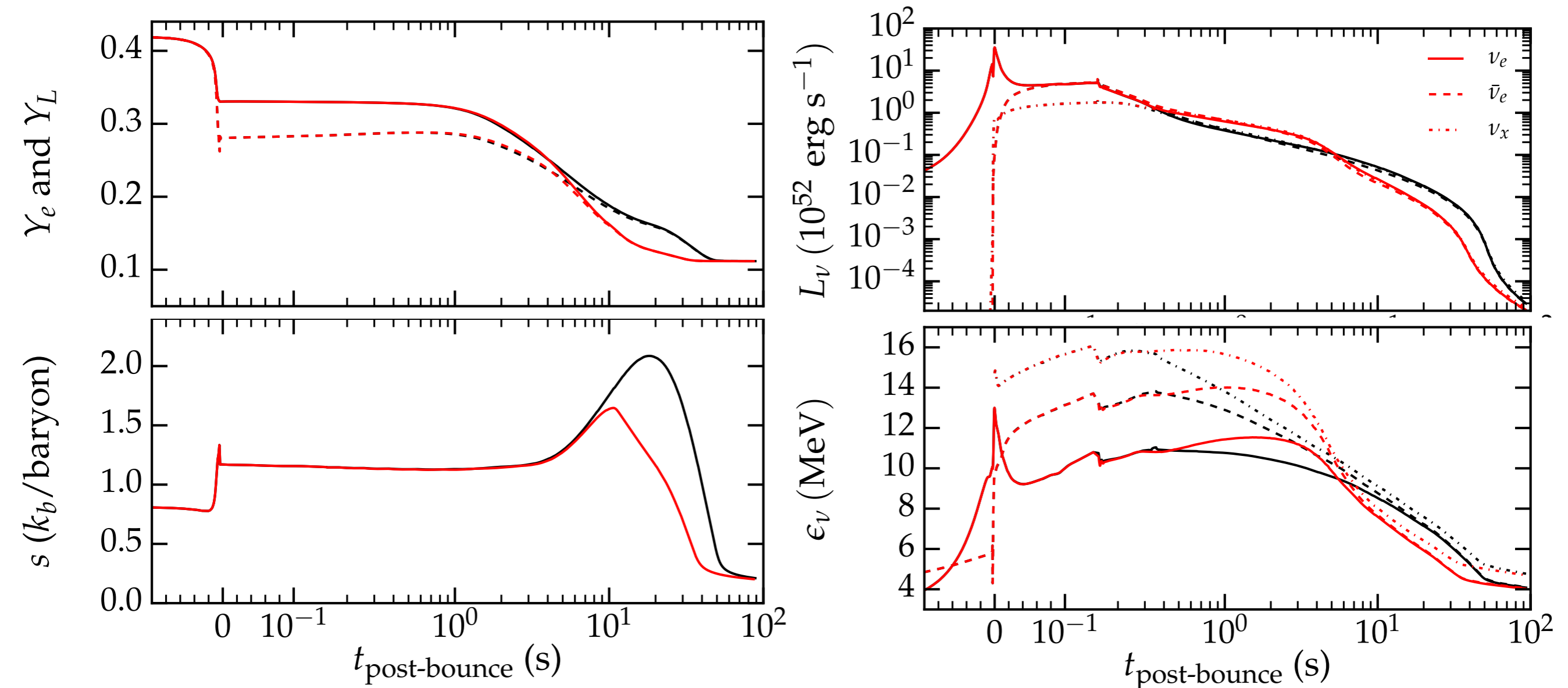
Region of convective instability determined by the Ledoux Criterion:

$$C_L = - \left( \frac{\partial P}{\partial s} \right)_{n, Y_l} \frac{ds}{dr} - \left( \frac{\partial P}{\partial Y_l} \right)_{n, s} \frac{dY_l}{dr} > 0$$

# Convection Conditions



# Convection



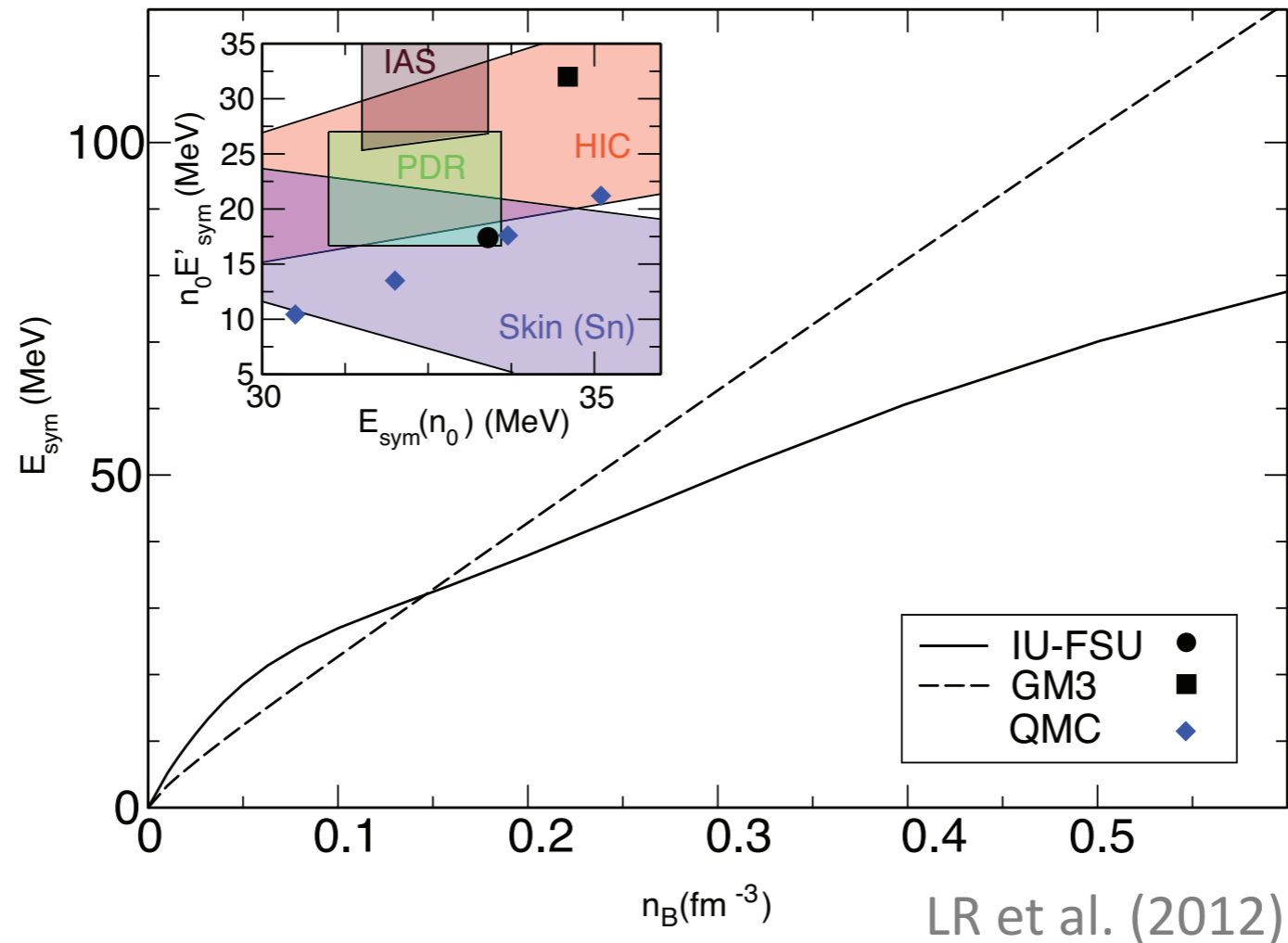
Black: No Convection

Red: Convection

See also Mirizzi et al. (2015)

# Proto-Neutron Star Convection

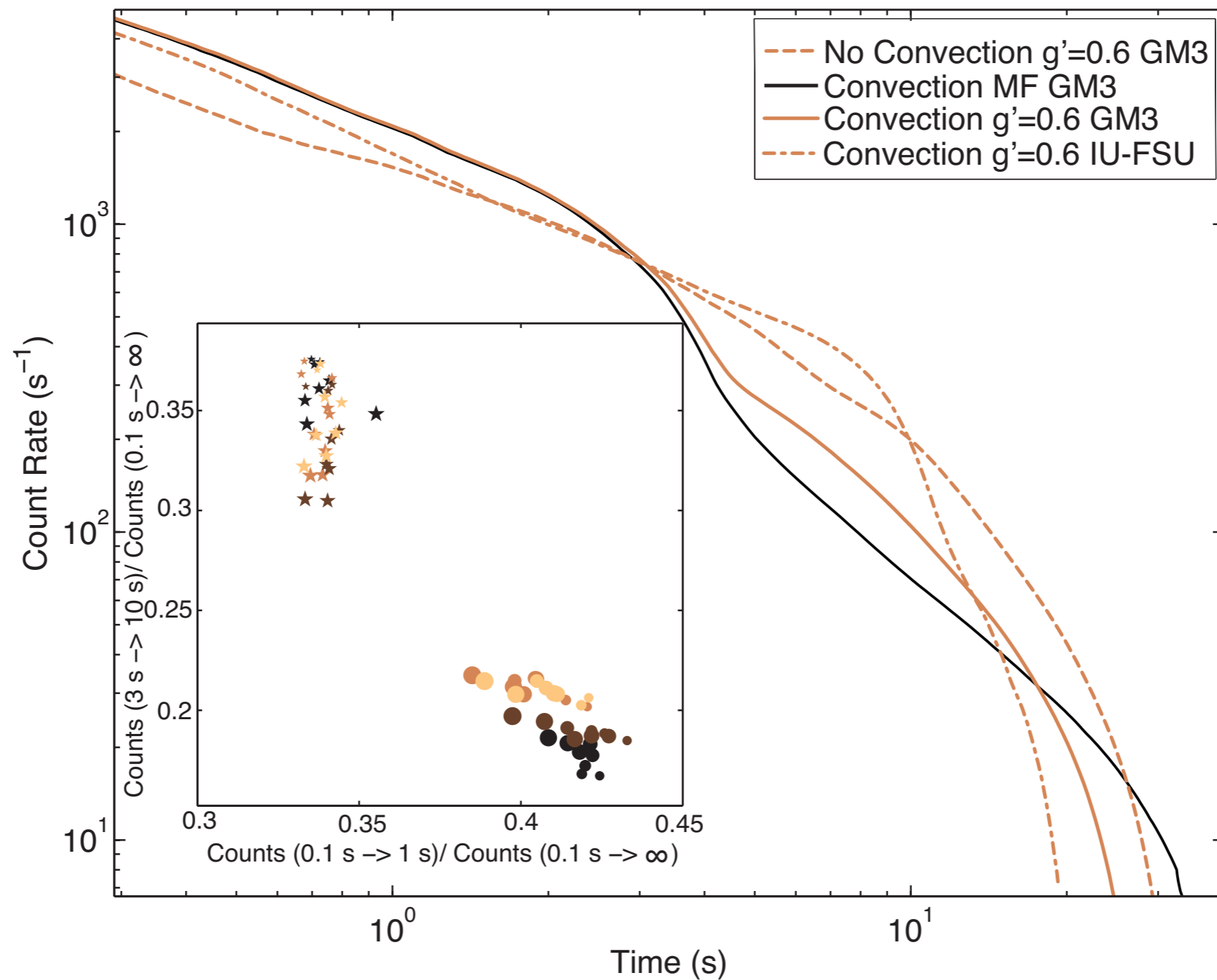
## Dependence on the EoS



Pressure derivatives are sensitive to the symmetry energy derivative:

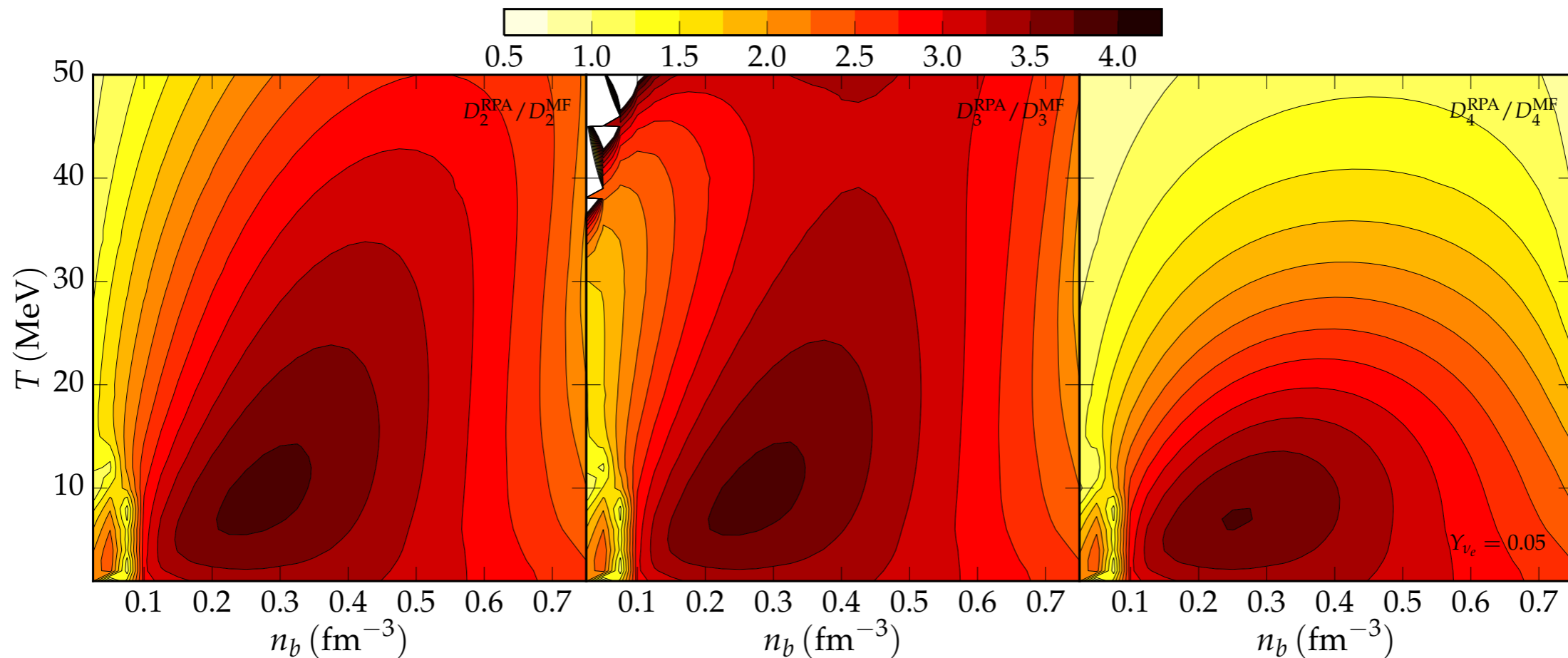
$$\left( \frac{\partial P}{\partial Y_L} \right)_{n_B} \simeq n_B^{4/3} Y_e^{1/3} - 4n_B^2 E'_{\text{sym}}(1 - 2Y_e)$$

# Comparison of Count Rates including Convection and Opacity Corrections



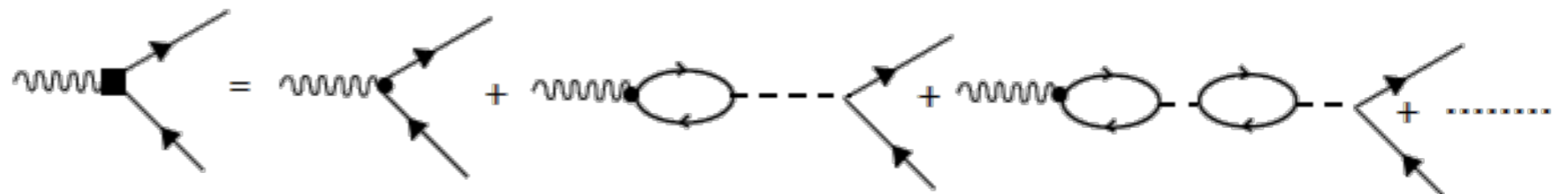
# Impact of Nuclear Correlations on Neutrino Opacities

See Horowitz '93, Reddy et al. '99, and Burrows & Sawyer '99



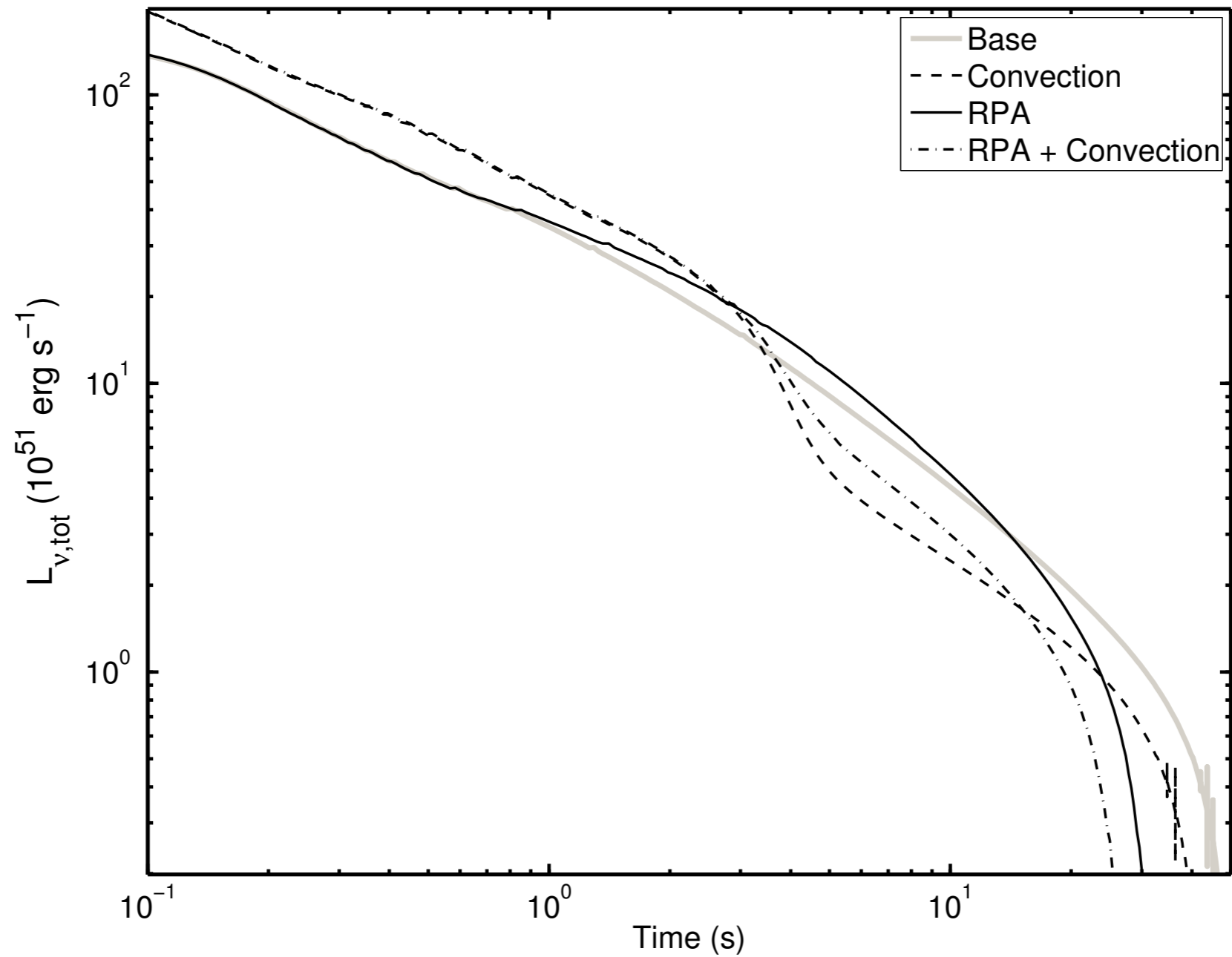
## Neutrino Diffusion Coefficients

Correlations through the RPA:



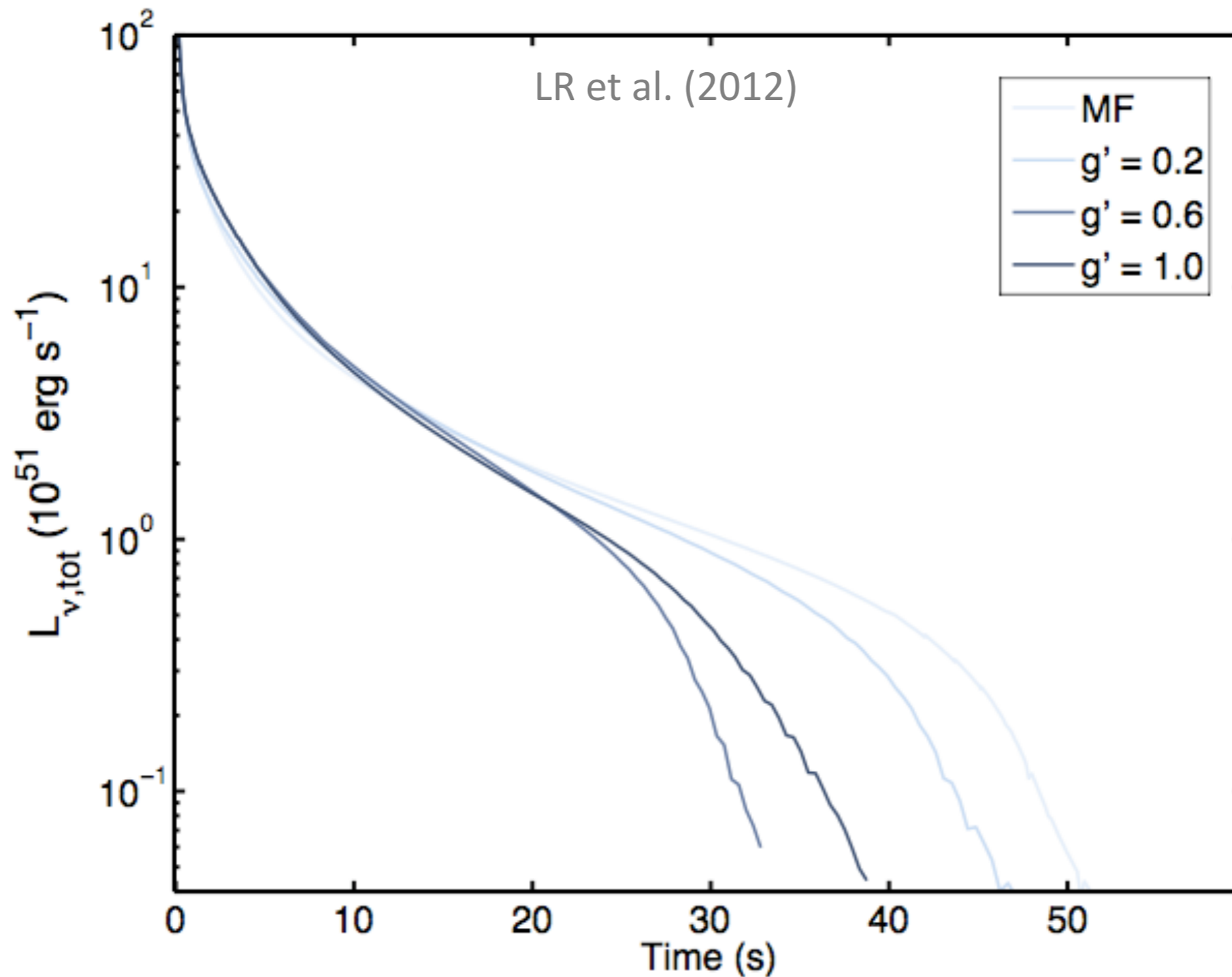


# Impact of Screening



LR et al. (2012)  
see also Huedepohl et al. (2010)

# Variations in the Interaction

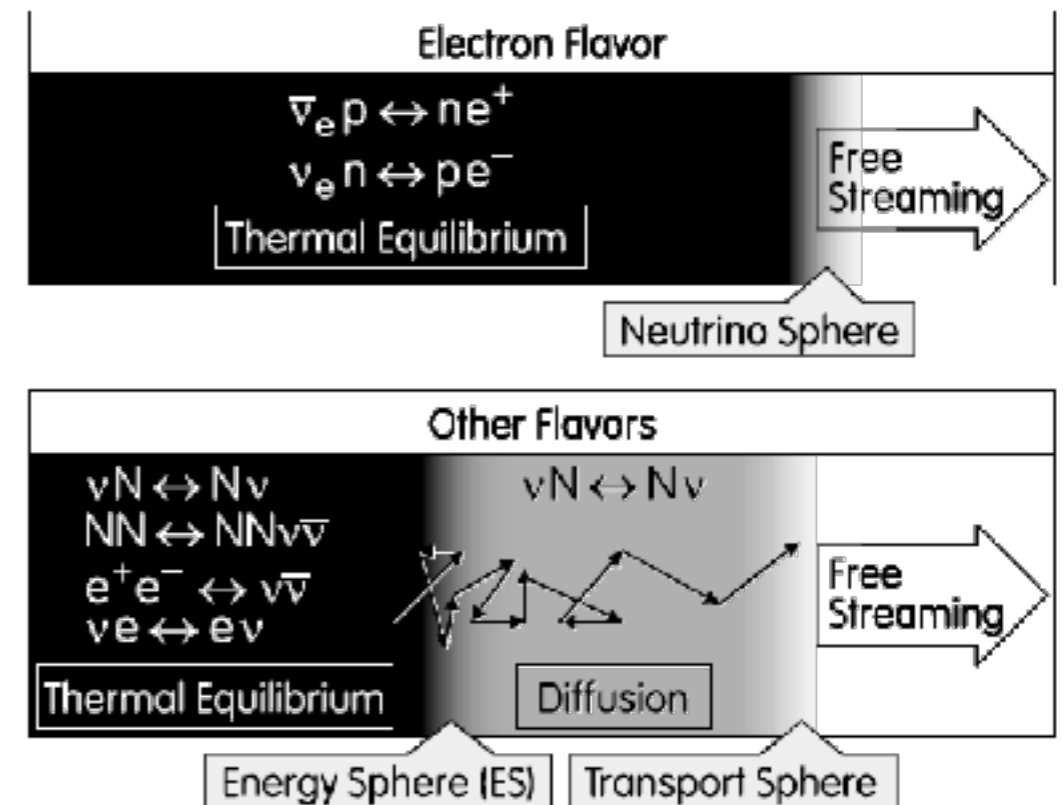


Varying the axial vector coupling

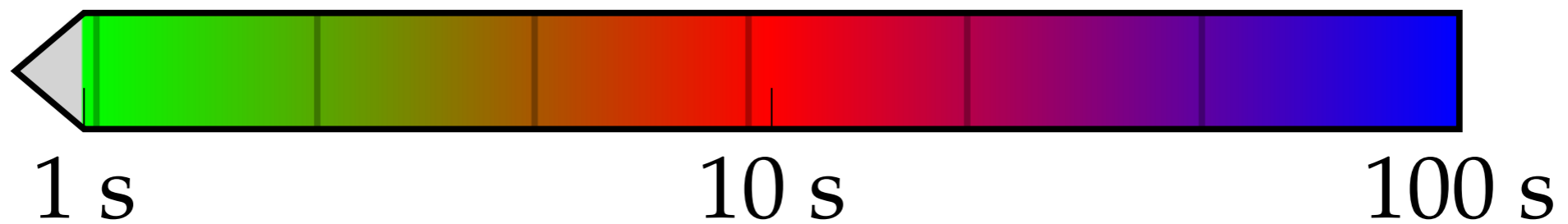
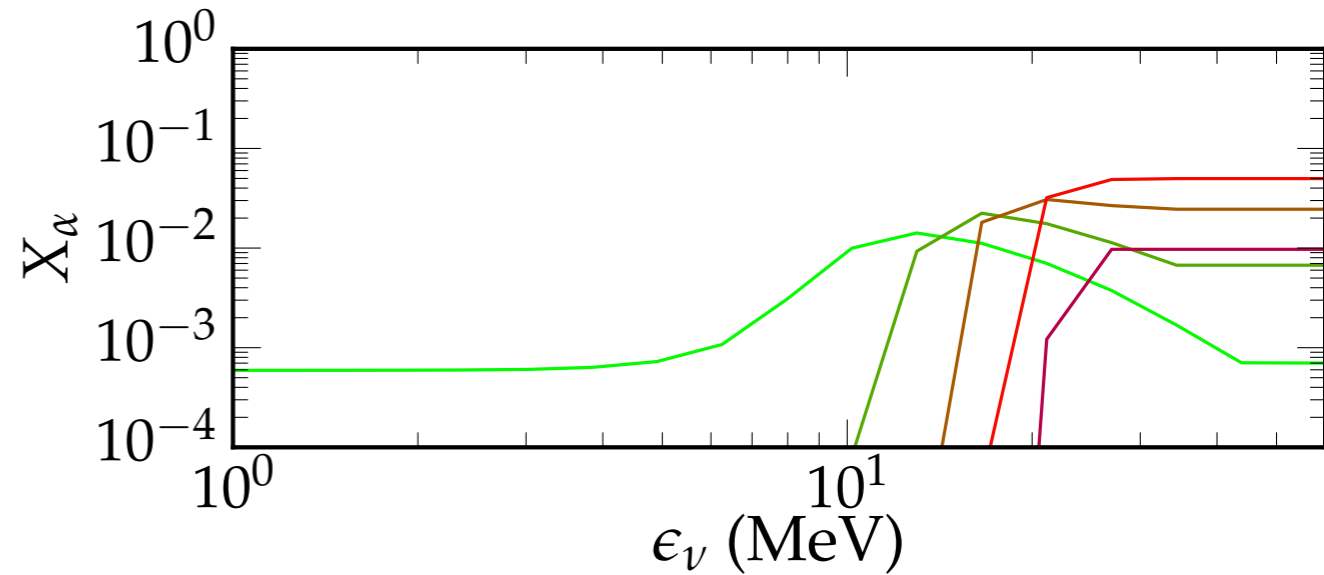
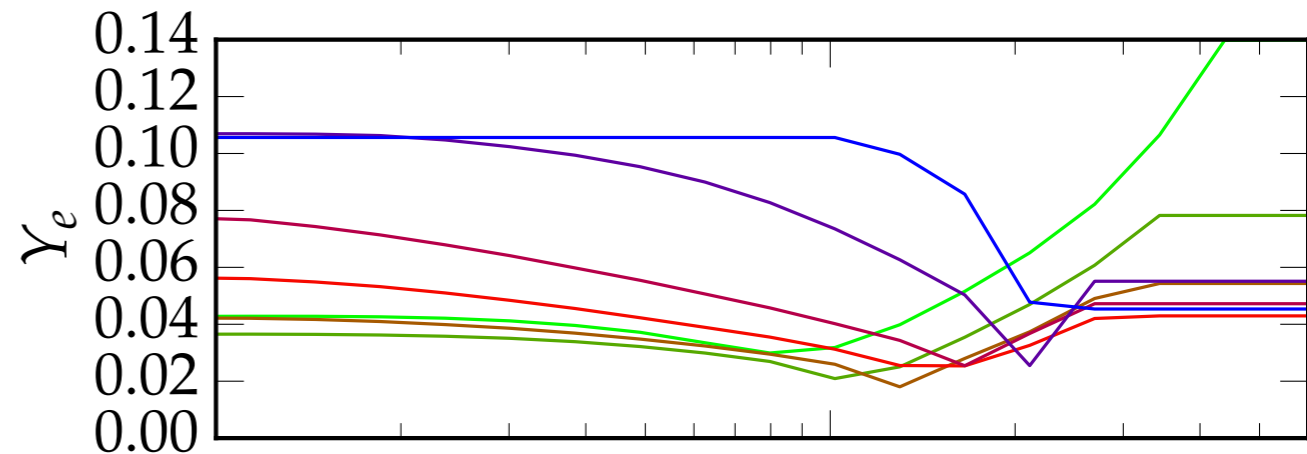
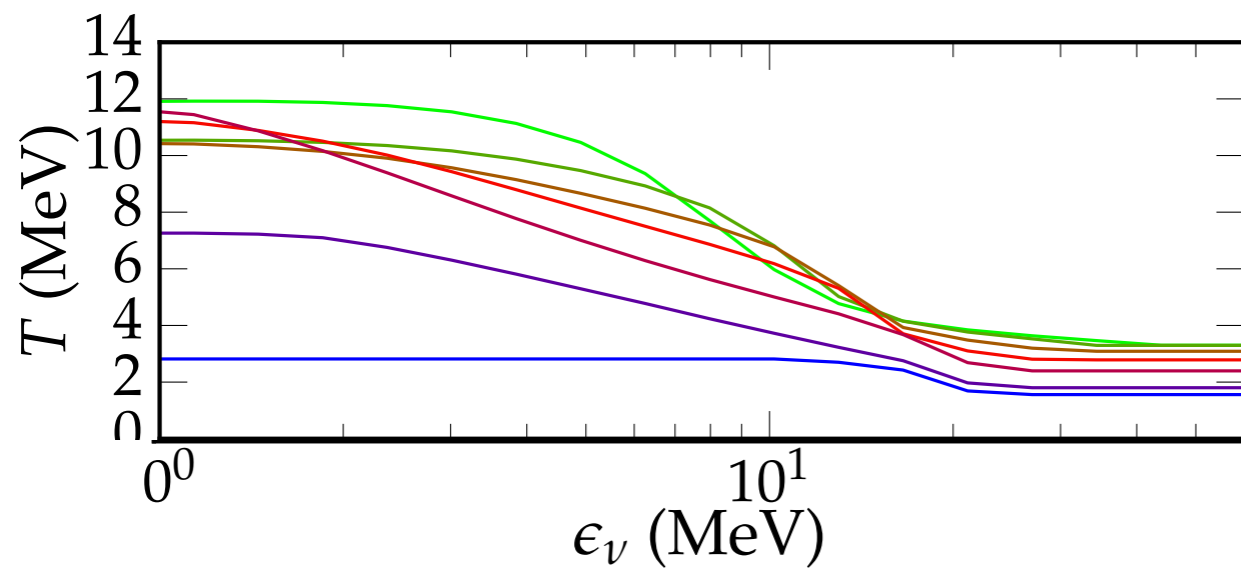
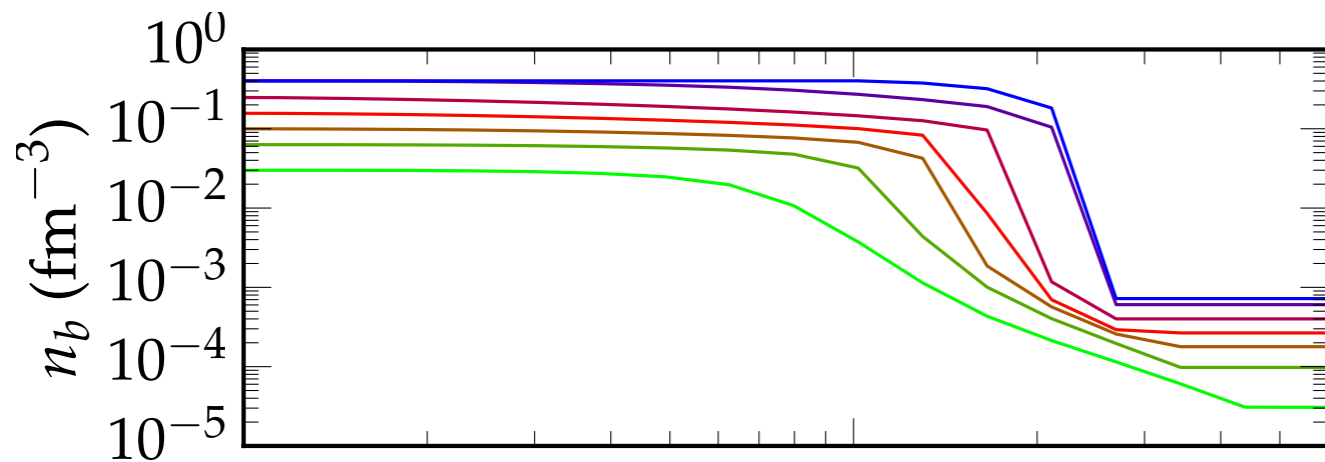
Reddy et al. (1999)

# What Determines the $\nu_e$ Spectra?

- “Neutrino sphere” is not well defined, energy dependent, range of densities and temperature
- Both charged and neutral current reactions important to  $\nu_e$  and anti- $\nu_e$  decoupling radii
- Charged current rates introduce asymmetry between neutrinos and antineutrinos
- Difference between  $\nu_e$  and anti- $\nu_e$  spectra strongly influences electron fraction of the neutrino driven wind and the nucleosynthesis that occurs there



# Decoupling Conditions



# Charged Current Interaction Rates in Medium

Nucleons are in an interacting medium, have altered dispersion relations:

$$E_i(k) = \sqrt{k^2 + M^{*2}} + U_i$$

Transfers potential difference to outgoing leptons:

$$\Delta U = U_n - U_p \approx 40 \times \frac{(n_n - n_p)}{n_0} \text{ MeV}$$

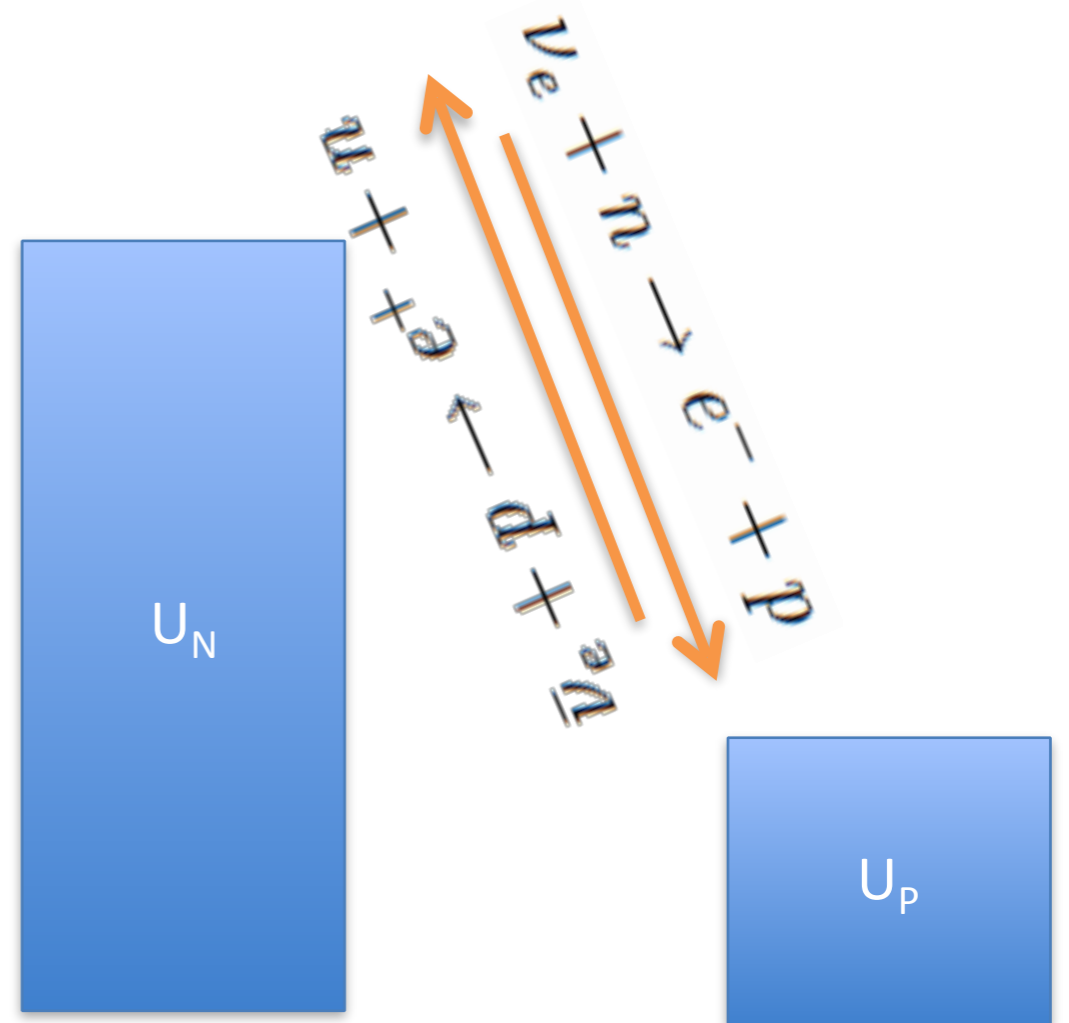
$$E_e = E_\nu + \Delta U$$

$$\frac{1}{V} \frac{d^2\sigma}{d\cos\theta dE_e} \propto \frac{G_F^2 \cos^2\theta_c}{4\pi^2} p_e E_e (1 - f_e(E_e))$$

Exponential increase in available phase space for electron neutrino capture:

$$\frac{\lambda^{-1}(\Delta U)}{\lambda^{-1}(\Delta U = 0)} \approx \frac{(\epsilon_\nu + \Delta U)^2}{\epsilon_\nu^2} \exp(\Delta U / T)$$

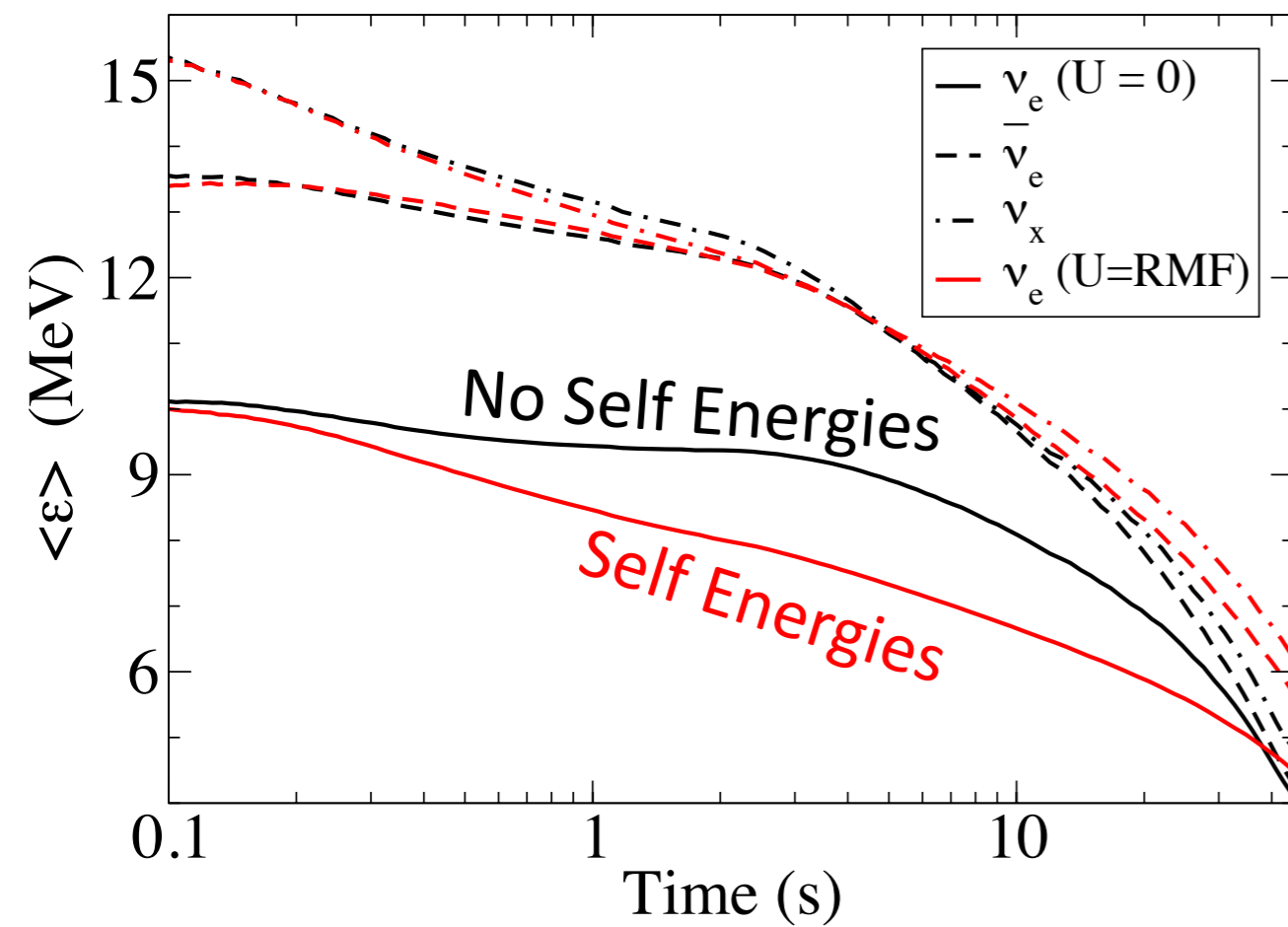
e.g. Reddy et al. 1998,  
Horowitz & Perez-Garcia 2003,  
LR, Reddy & Shen 2012,  
LR & Reddy 2017



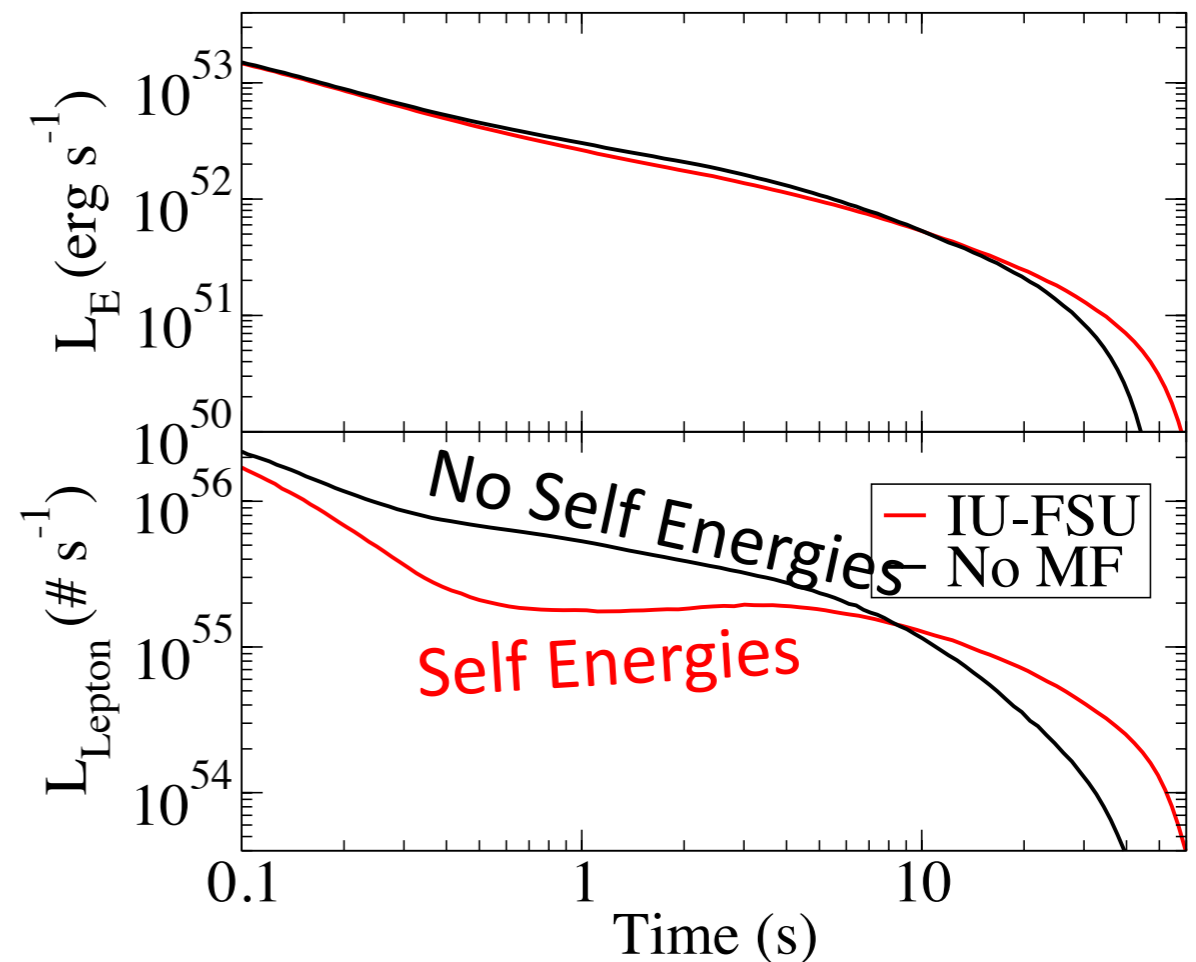
# Neutrino emission w/ and w/o Nuclear Interactions

See LR '12 and Martinez-Pinedo et al. '12

Self energies shift average neutrino energies

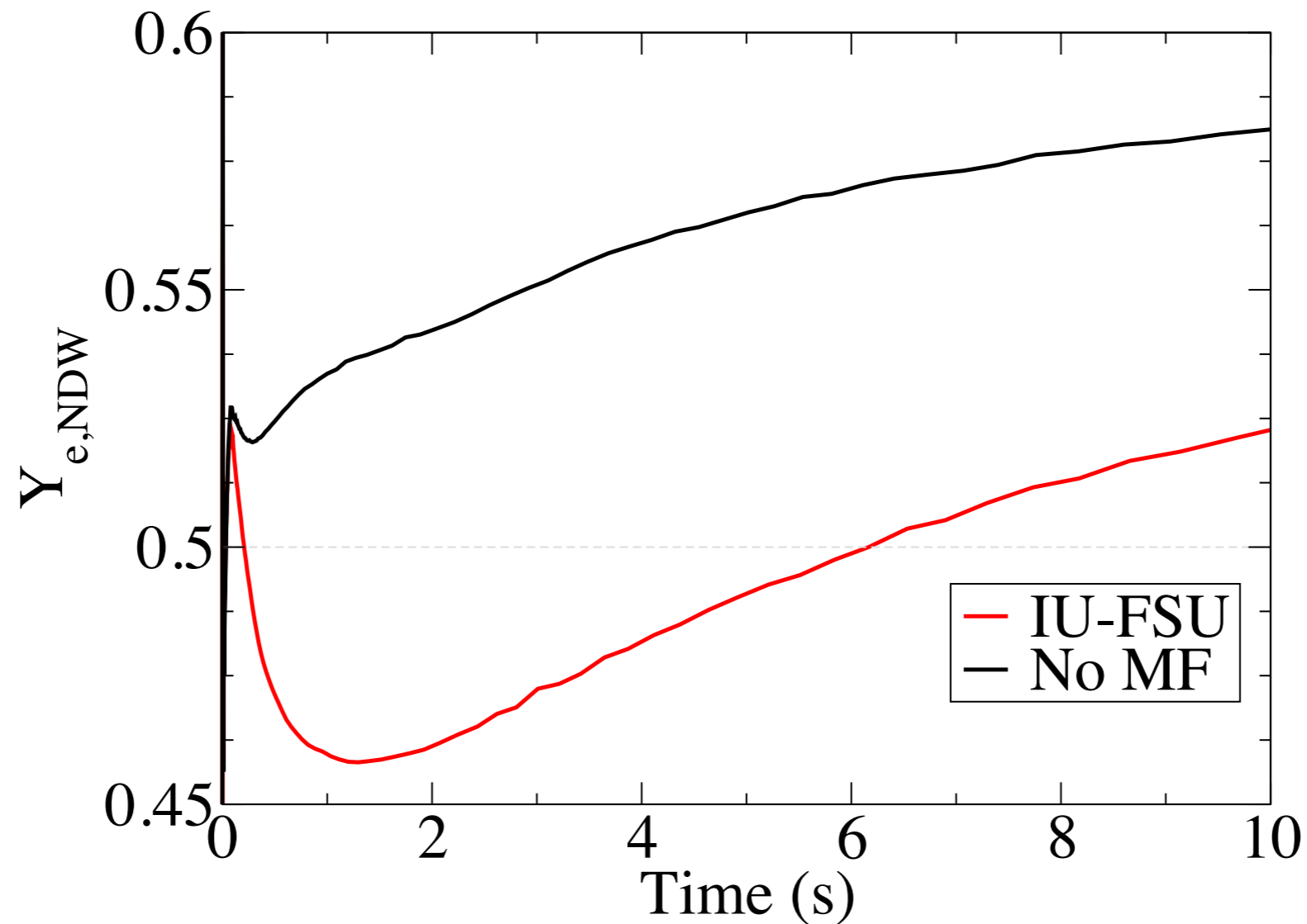


Deleptonization



# Neutrino emission w/ and w/o Nuclear Interactions

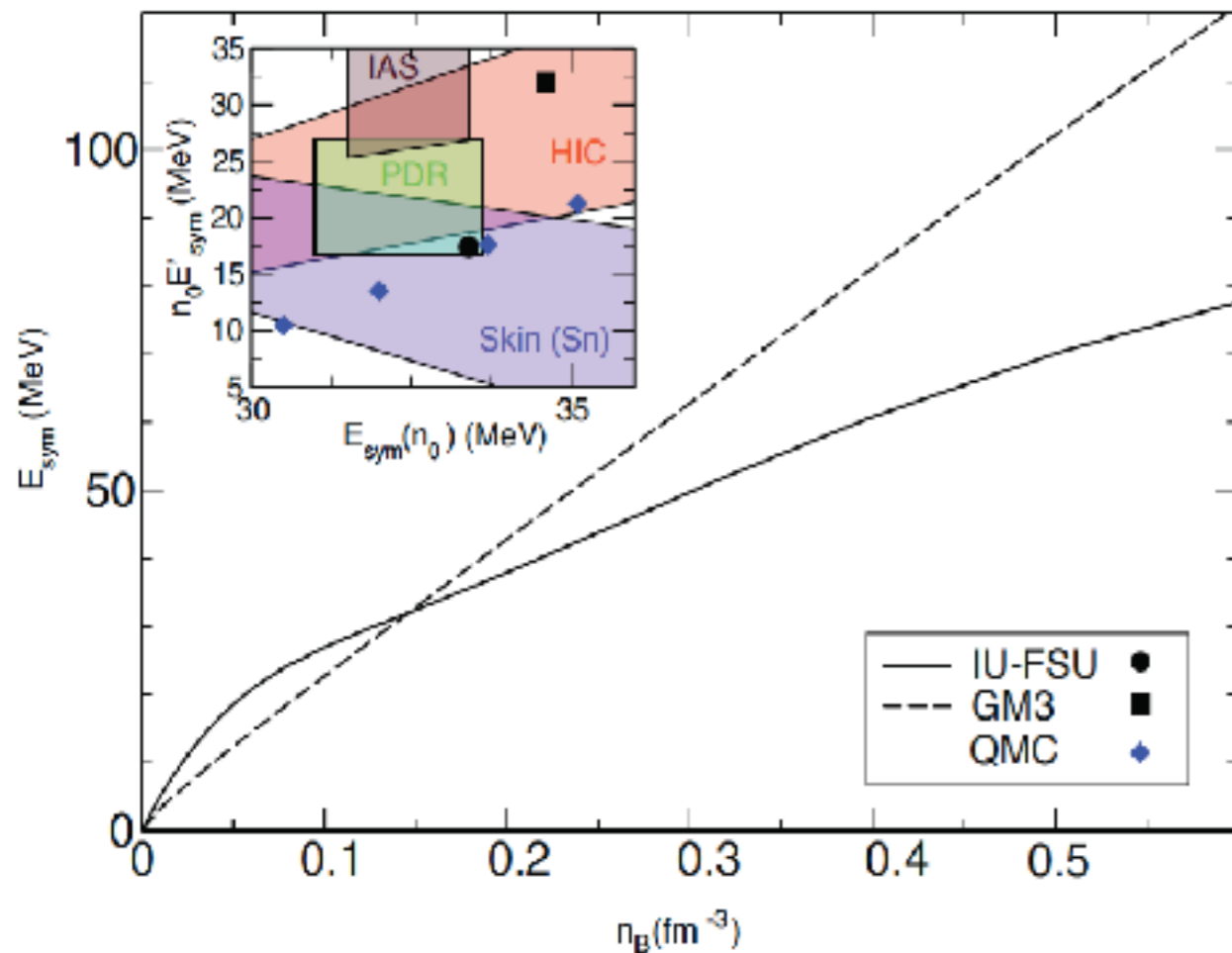
See LR '12 and Martinez-Pinedo et al. '12



$$Y_e \approx \frac{\lambda_{\nu_e}^{-1}}{\lambda_{\nu_e}^{-1} + \lambda_{\bar{\nu}_e}^{-1}} \approx \left( 1 + \frac{\dot{N}_{\bar{\nu}_e}}{\dot{N}_{\nu_e}} \frac{(\epsilon_{\bar{\nu}_e} - \Delta)^2}{(\epsilon_{\nu_e} + \Delta)^2} \right)^{-1}$$

# Symmetry Energy Dependence

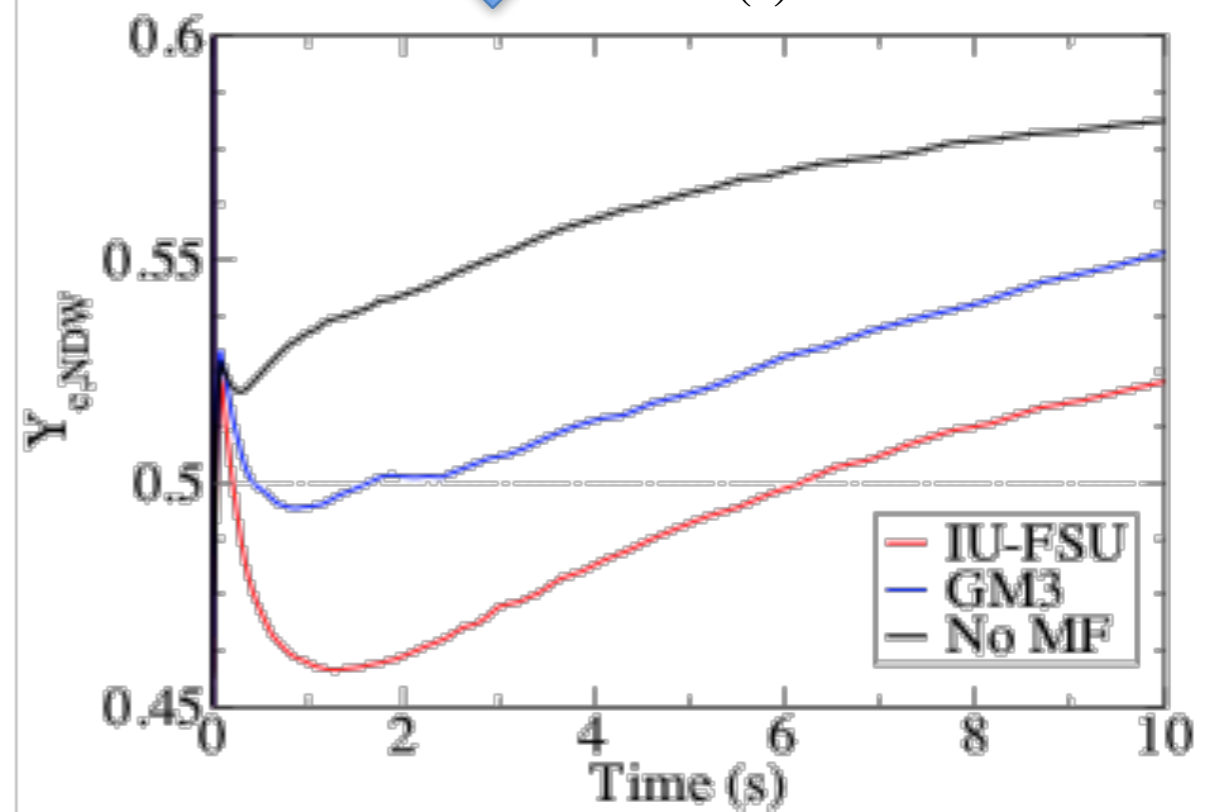
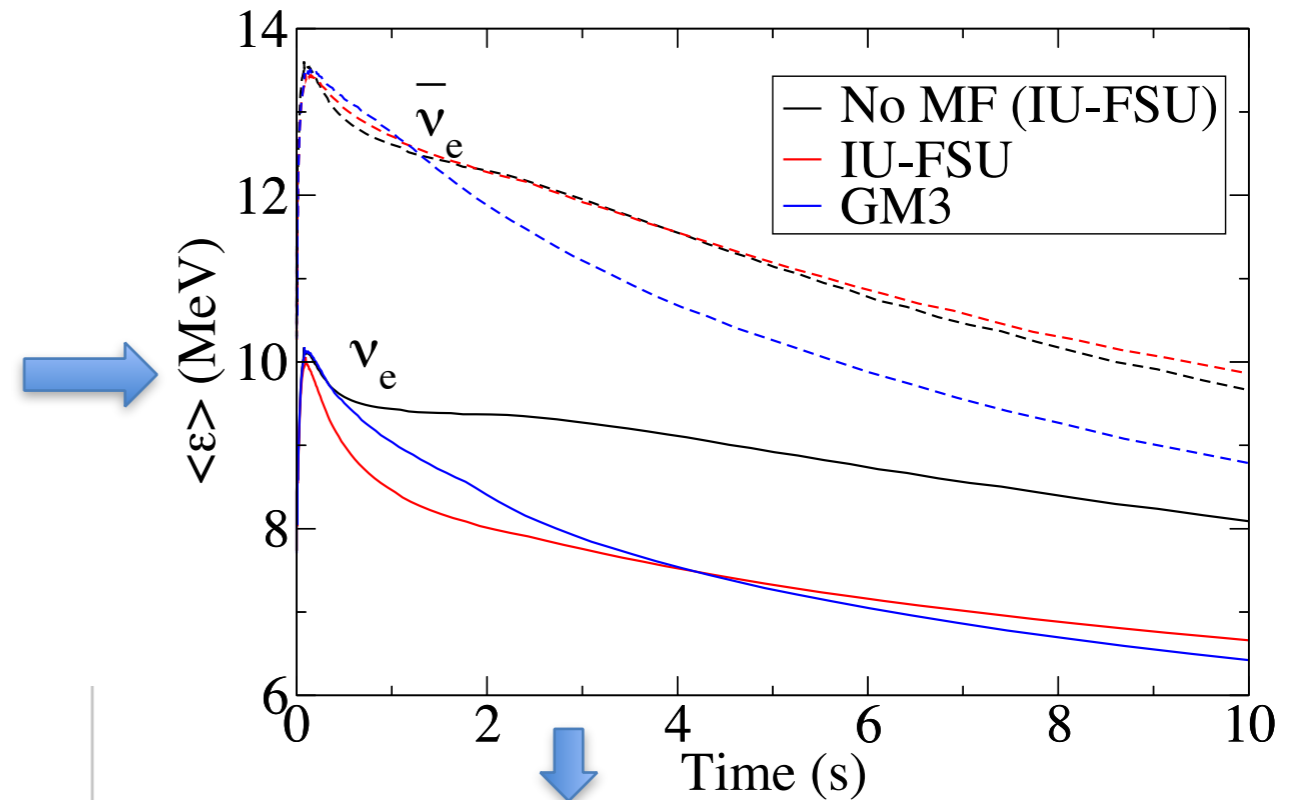
From Roberts et al. (2012)



Different equations of state

Model	$\Delta U$ (MeV)
Lowest order virial, Eq. (21)	3.85
Virial $\mu_i - \mu_i^f$ , Eq. (31)	2.27
Mean field model GM3, Eq. (36)	0.23
Mean field model IUFSU [24]	1.11

From Horowitz et al. (2012)





# Conclusions

- PNS convection significantly impacts the neutrino cooling timescale, produces a break in the neutrino emission. Convection is sensitive to the nuclear EoS (mainly the symmetry energy), so constraining density dependence is important to predicting the timescale of neutrino emission
- Neutrino opacities especially important to the late time cooling timescale. In particular, nuclear correlations can also leave a signature on the tail of the neutrino signal.
- Properties of the neutrinos can also impact nucleosynthesis near the PNS. The nucleon self-energies play a significant role in determining neutron or proton richness of the NDW.